Course Logistics

1. 4 Quizzes — 12%
   (no make up Qs)
2. 4 Assignments — 28%
   (mandatory — all of them)
3. Minor Exam — 30%
4. Major Exam — 30%

- Attendance in Exams Compulsory

Introduction to logic & Functional Programming

- Quickly about the course
  - Various programming paradigms
    - functional, imperative, logic, & OOP

- for types
- technique for language description

Model of Computation

- Expression Interpreter
  i.e. function applied to subexpressions
- Sequence of actions on an underlying m/c
- Constraint calculus | on relations → deduce new inferences
- independent objects to interact by sending msgs to each other

- Language can be described by writing a def^r interpreter
  Eg: LISP
  - Language Description & Implementation
    - syntax + definitional interpreter
      - lambda calculus → A convenient vehicle to study hofunctions, types etc.
  - Concepts from compilers and software Engineeri

Poll

- How many know functional programming
- How many know logic & logic programming?
- Have you used recursion?
- How comfortable are you with mathematical induction?

Lec 1

- What is a computation?
  - A: a finite sequence of transformations by means of predefined rules on finite & discrete data

Eg: $f(x) = x+1$,

Q: What is a non-computation?
- → finding a poem?
- → specified with the help of programs

And what is computable?

- What is an algorithm?
  - → a finite seqe of instr. solving a problem
- What is a program? And programming?
  - → Representation of an alg. in a lang.
  - → Logical aspects of program organization
    - → D.S. choice, Modularity, Reuse etc.

The choice of programming language is important!

→ It determines the kind of computations that can be carried out!

Eg: Computational model consists of a ruler + compass

→ what we can compute?

→ bisect an angle, $\sqrt{n}$, ... etc.

→ what we cannot do?

→ trisect an angle

Need additional things in our model of computation such as protractor.

Other Computational tools

- Abacus (still used in Japan)
- Paper & pencil
- Stick & stones
- ⋮

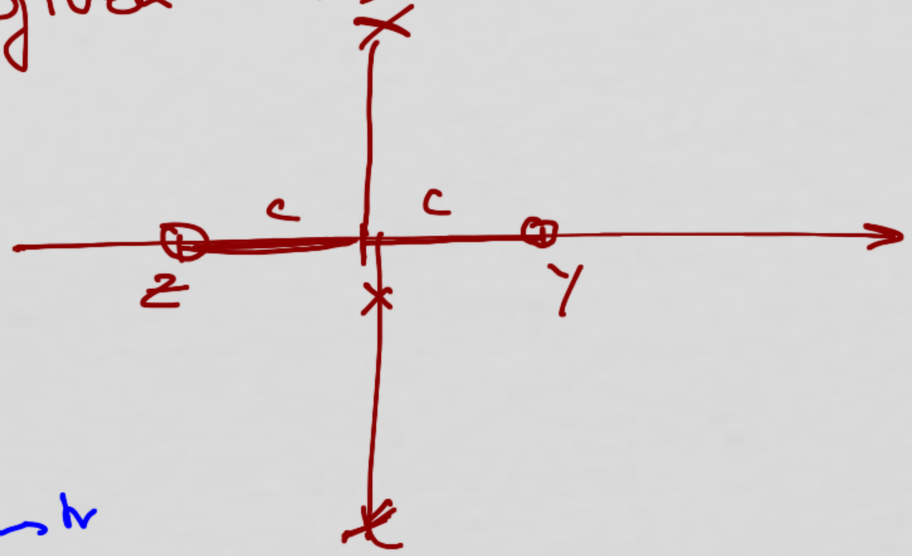
→ Programming languages (model of computation)
that can be turing complete with
goto and if..then-else
→ HTML turing complete?
→ Regular expression turing complete?

→ Computationally Universal → anything that is computable via an algorithm can be made to run on a turing m/c.

In summary every computational model must have
- primitive ops & exprs which represent the simplest objects with which the model is concerned
- Methods of combination: how to combine primitive ops to get compound exprs

- Methods of abstraction: how to use compound exprs as named units.

Eg: Perpendicular at a pt (x)
↳ given a line



Steps

1. Mark Y & Z at c units from X
2. Draw circles
   C_1 (Z, 2c)
   C_2 (Y, 2c)
3. Join the pts of intersection of two circles

Using 1 const to construct a square → Method of abstraction

Program specification

- How do we specify what to expect from a program?
- How do we map what we expect from the program & what the program really computes?
- How do user ensure program is correct vis-a-vis its specification

Ans: Rigorously answered by means of formal mathematical specification & a formal relationship both spec & prog.

PL History

→ invented to make easier use of m/c

→ Can be both higher-level & general purpose

I. Machine Language → lowest level (Von Neumann m/c 1946)

→ virtually unintelligible

II Assembly Language → Variant of Machine language but with Mnemonics,

[i.e. names of m/c ops symbols for values, storage locations etc.

Readable but tied to a m/c arch.

[No m/c independence]

III Fortran (formula translator)

↓

first compiler, [therefore m/c independence]

Availability of libs

↳ portability

IV LISP (List processor)

(interpreters)

Exp. evaluators

i.e. symbolic manipulator

Interpreters → High level m/cs

Prolog

(Abstract m/cs)

Logical inference

V Algol

⋮

PASCAL

⋮

C/C++

Compiler on a V.M.

Compilers are translators

Functional Programming

- S/w becoming complex, becoming more important to structure it well

- Conventional languages place conceptual limits on the way problems can be modularised

- In F.P. — functions are treated as mathematical functions

  which

  means

- No assignment statements

$$x := x + 1$$

Referentially transparent → Expr ⇔ values → No change in the behavior of the program

→ Thus a variable given a value can never change

→ Variables are treated as Constants

→ More generally,

→ As a result common compiler opt. such as subexpression elimination, Code movement etc do not require fixpt data-flow analysis

** Major source of bugs → no side-effects

Also → No sideeffects ⇒ no need to define prescribe flow of control

↳ program becomes traetable mathematically

- No iteration loops
  ↳ instead recursion is used
  [Theory behind it is induction]

- Higher order functions
  ↳ leads to compact & concise code

Note: I/O is inherently imperative